

Strong Thermopower Enhancement and Tunable Power Factor *via* Semimetal to Semiconductor Transition in a Transition-Metal Dichalcogenide

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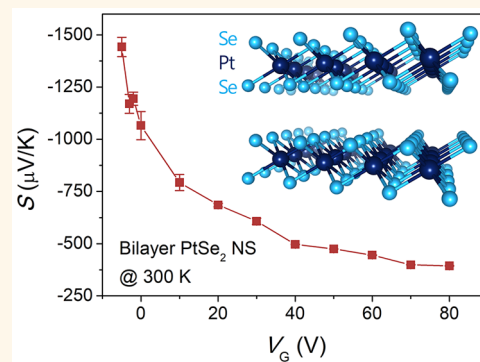
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Supporting Information

ABSTRACT: Electronic band engineering is a promising approach to enhance the thermopower of thermoelectric materials. In transition-metal dichalcogenides (TMDCs), this has so far only been achieved using their inherent semiconducting nature. Here, we report the thickness-modulated band engineering of nanosheets based on semimetallic platinum diselenide (PtSe₂) resulting in a thermopower enhancement of more than 50 times than that of the bulk. We obtained this by introducing a semimetal to semiconductor (SMSC) transition resulting in the formation of a bandgap. This approach based on semimetallic TMDCs provides potential advantages such as a large variation of transport properties, a decrease of the ambipolar transport effect, and a high carrier density dependence of the transport properties. Our observations suggest that the SMSC transition in TMDCs is a promising and straightforward strategy for the development of two-dimensional nanostructured thermoelectric materials.

KEYWORDS: transition-metal dichalcogenides, platinum diselenide, electronic band engineering, semimetal to semiconductor transition, thermopower



To improve the energy conversion efficiency of thermoelectric materials, significant effort has been placed on developing various nanostructures.^{1–3} Crucial properties of a thermoelectric material are the thermopower, also referred to as Seebeck coefficient S , and the electrical conductivity σ .⁴ To achieve a significant enhancement of the thermoelectric power factor ($S^2\sigma$), it has first been proposed to use one- and two-dimensional bismuth structures and take advantage of their quantum confinement effect on electrons.^{5,6} However, it has been gradually recognized that to boost thermoelectric performance, it is easier and more robust to suppress the thermal conductivity of a material using phonon scattering at interfaces and boundaries in nanostructures.^{7–10} Another approach to enhance the power factor is to alter the electronic band structures of a material by nanostructuring, which is called band engineering.^{11–17} In particular, one-dimensional semiconducting and semimetallic nanowires have been intensively investigated^{12,13} because the

thermopower is extremely sensitive to band structures and the asymmetries of electrons and holes in materials.¹⁴ However, only few studies have demonstrated a thermopower enhancement using nanowires beyond that of the bulk material.^{15–17}

Recently, semiconducting two-dimensional transition-metal dichalcogenide (TMDC) nanosheets have attracted great interest to obtain enhanced power factors owing to the presence of intrinsic bandgaps and the potential to modulate the band structures by changing their thickness.^{18–24} The power factor enhancement was successfully demonstrated in semiconducting bilayer nanosheets of WSe₂, MoS₂, and black phosphorus using field effect gating, achieving values comparable to that of commercial bulk Bi₂Te₃.^{18–20} However,

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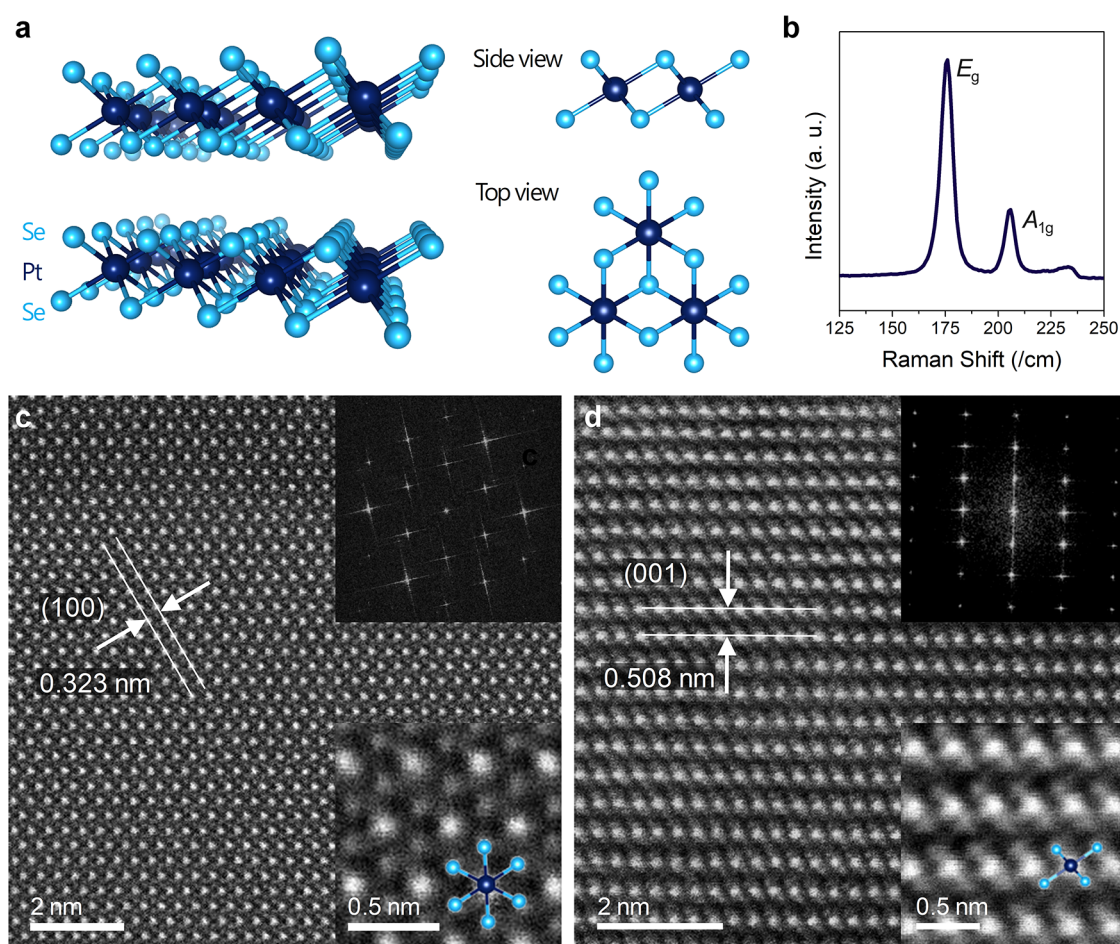


Figure 1. Characterization of the PtSe₂ nanosheets. (a) Schematic crystal structure of a bilayer PtSe₂ nanosheet (left), and side and top views of the 1T phase PtSe₂ crystal structure (right). The dark blue and light blue spheres represent Pt and Se atoms, respectively. (b) Raman spectrum of a PtSe₂ nanosheet. (c, d) HR-STEM images of a mechanically exfoliated PtSe₂ nanosheet (c) and a cross-sectional specimen (d). The insets are the Fourier transforms of the respective HR-STEM images (top) and the corresponding high-magnification HR-STEM images (bottom).

the thermopower of the nanosheets has not been shown to exceed that of bulk crystals^{25,26} even when utilizing the gate effect. Similarly, in theoretical studies based on MoS₂, MoSe₂, WS₂, WSe₂, SnS₂, and TiS₂ nanosheets, the power factor was found to increase with decreasing thickness, but the dramatic thermopower enhancement predicted based on their electronic band structure could not be obtained.^{21–24} In fact, the power factor enhancement has so far only been observed using field effect gating in 2D semiconducting TMDCs that have an inherently high thermopower.^{18–20}

Here, we report on the significant thermopower enhancement in a semimetallic TMDC by introducing a semimetal to semiconductor (SMSC) transition.^{6,16} We systematically investigated two-dimensional nanosheets exfoliated from semimetallic platinum diselenide (PtSe₂) crystals and obtained thermopowers higher than 1 mV/K. The semiconducting PtSe₂ nanosheets obtained by the SMSC transition provide potential advantages in terms of band engineering efficiency for thermoelectric applications. First, the variation of transport properties is exceptionally large compared to that of the bandgap modulation because of the sudden splitting between the overlapping conduction and valence bands. Second, the ambipolar charge carrier transport problem, in which the contributions of electrons and holes to the thermopower offset

each other, is diminished by the bandgap formation, and thus, the thermopower enhancement can be further promoted. Third, the transport properties become further sensitive to the intrinsic properties such as carrier density, and thus the thermoelectric properties can be effectively optimized by the field effect gating and extrinsic doping. Our findings represent an approach of thickness-modulated band engineering for thermoelectric applications, which we anticipate to be universally adaptable for semimetallic TMDCs.

RESULTS AND DISCUSSION

Single-Crystalline 1T Phase PtSe₂ Nanosheets. PtSe₂ nanosheets were obtained using a mechanical exfoliation method on 300 nm SiO₂/Si substrates. Each PtSe₂ layer consists of three atomic sublayers, in which platinum (Pt) atoms are sandwiched between selenium (Se) atoms (Figure 1a).^{27,28} We performed Raman spectroscopy to confirm the phase of the PtSe₂ nanosheets. We observed two pronounced peaks centered around 175 and 206 cm⁻¹ (Figure 1b), which correspond to the E_g and A_{1g} Raman active modes originating from the vibration of Se atoms. This is consistent with a previous study on the single-crystalline 1T phase PtSe₂.²⁹ We also observed the infrared active modes A_{2u} and E_u due to vibrations of Pt and Se atoms at around 230 cm⁻¹. In order to

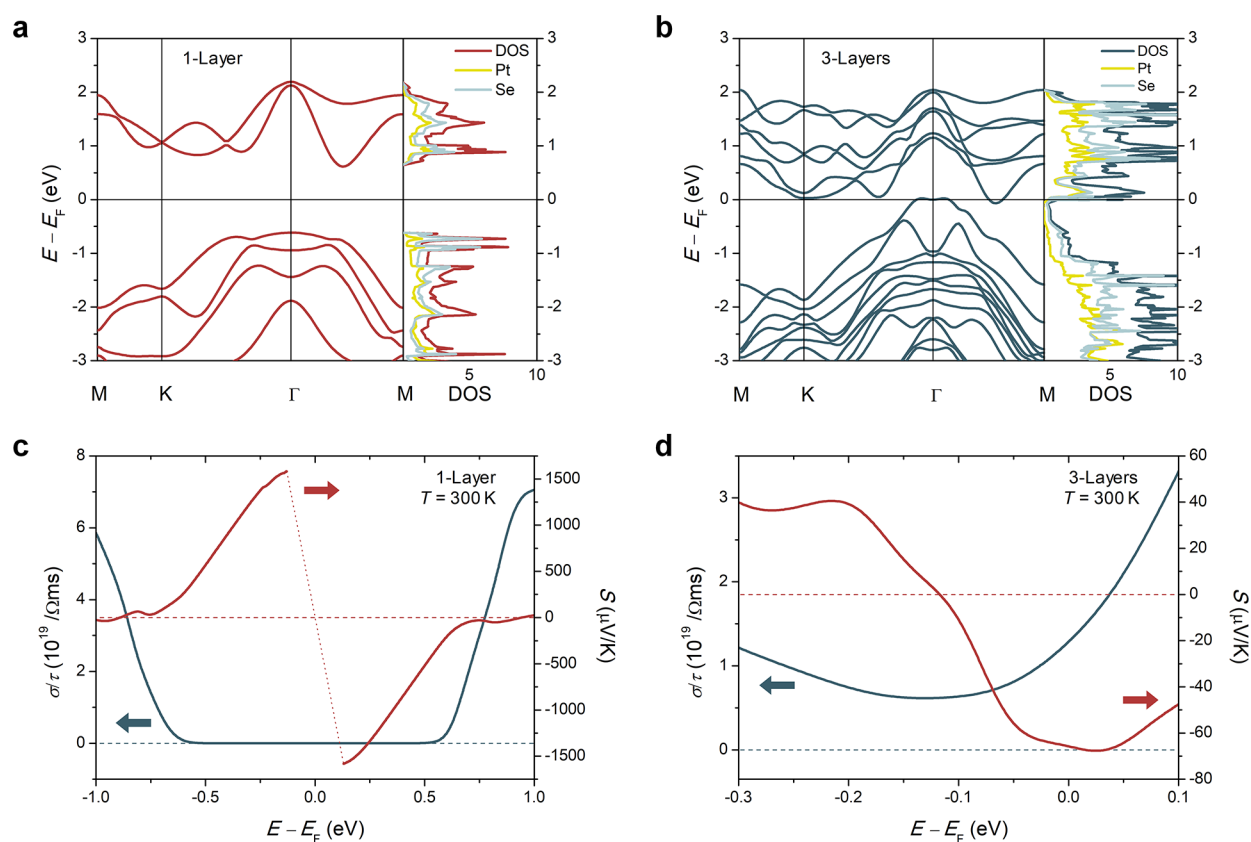


Figure 2. Theoretical calculation of the electronic properties of the PtSe₂ nanosheets. (a, b) Electronic band structures and DOS of monolayer (a) and trilayer (b) PtSe₂ nanosheets. (c, d) Electrical conductivity (σ) with respect to scattering time (τ) (dark blue) and thermopower (S) (red) of the monolayer (c) and trilayer (d) nanosheets as a function of the energy at room temperature. The horizontal dashed lines indicate zero-electrical conductivity (dark blue) and zero-thermoelectric power (red). The red dotted line indicates the range where no thermopower could be obtained.

investigate the crystal structure of our samples, we performed high-resolution scanning transmission electron microscopy (HR-STEM). The top and side view HR-STEM images and corresponding Fourier transformation images indicate the single-crystalline nature of the mechanically exfoliated nanosheets (Figure 1c,d and top insets). High-magnification HR-STEM images clearly show bright Pt atoms each surrounded by six dark Se atoms (Figure 1c, bottom inset) and the layered structure of PtSe₂ (Figure 1d, bottom inset) indicating the 1T phase of the TMDCs.³⁰ The lattice constants were found to be $a = 0.373$ nm and $c = 0.508$ nm from the observed (100) and (001) plane spacings, which is in good agreement with a previous study.³¹

Semimetal to Semiconductor Transition in PtSe₂ Nanosheets. In order to calculate the thickness-modulated band structures and the critical thickness of the semimetal to semiconductor transition in PtSe₂ nanosheets, we performed first-principle calculations using density functional theory (DFT). We found that the band structure and density of states (DOS) of a monolayer PtSe₂ nanosheet represent those of an indirect semiconductor with a bandgap ($E_g = 1.23$ eV, Figure 2a), which is in good agreement with previous theoretical studies of the same system.^{27,30} In a bilayer nanosheet, the bandgap was reduced to 0.23 eV (Figure S1). In the trilayer nanosheet, conduction and valence bands started to overlap ($E_0 = 0.09$ eV, Figure 2b), thus exhibiting a semimetallic band structure. This is due to the new energy states originating from an extremely strong interlayer p_z orbital

hybridization of the Se atom, in which the antibonding p_z states are higher than the valence band maximum of a monolayer.³⁰ The band structure changed continuously with an increasing number of layers due to an increase of the antibonding p_z states. Bulk PtSe₂ exhibited a semimetallic band structure with an indirect band overlap of 0.87 eV (Figure S1).

To calculate the transport properties of monolayer and trilayer nanosheets, we solved the Boltzmann transport equation based on the DFT calculations (Figure 2c,d). In the monolayer nanosheet with a bandgap, the estimated electrical conductivity clearly showed semiconducting characteristics (Figure 2c). We predicted an enhancement of the thermopower above 1 mV/K near the conduction and valence band edges. The trilayer nanosheets with a semimetallic band structure, wherein electrons and holes coexist, exhibited ambipolar transport characteristics (Figure 2d). Near the overlapping bands, the electrical conductivity showed a minimum value without off (high resistance) state, and the thermopower changed signs by passing through zero thermopower. This is because the thermopower of electrons ($S < 0$) and holes ($S > 0$) offset each other.³² For this reason, in semimetals, a significant enhancement of thermopower is hardly observed. This limitation caused by the ambipolar transport effect can be dealt with by introducing an SMSC transition, which leads to the formation of a bandgap. Consequently, we found significant changes in transport characteristics when varying the thickness from bulk to

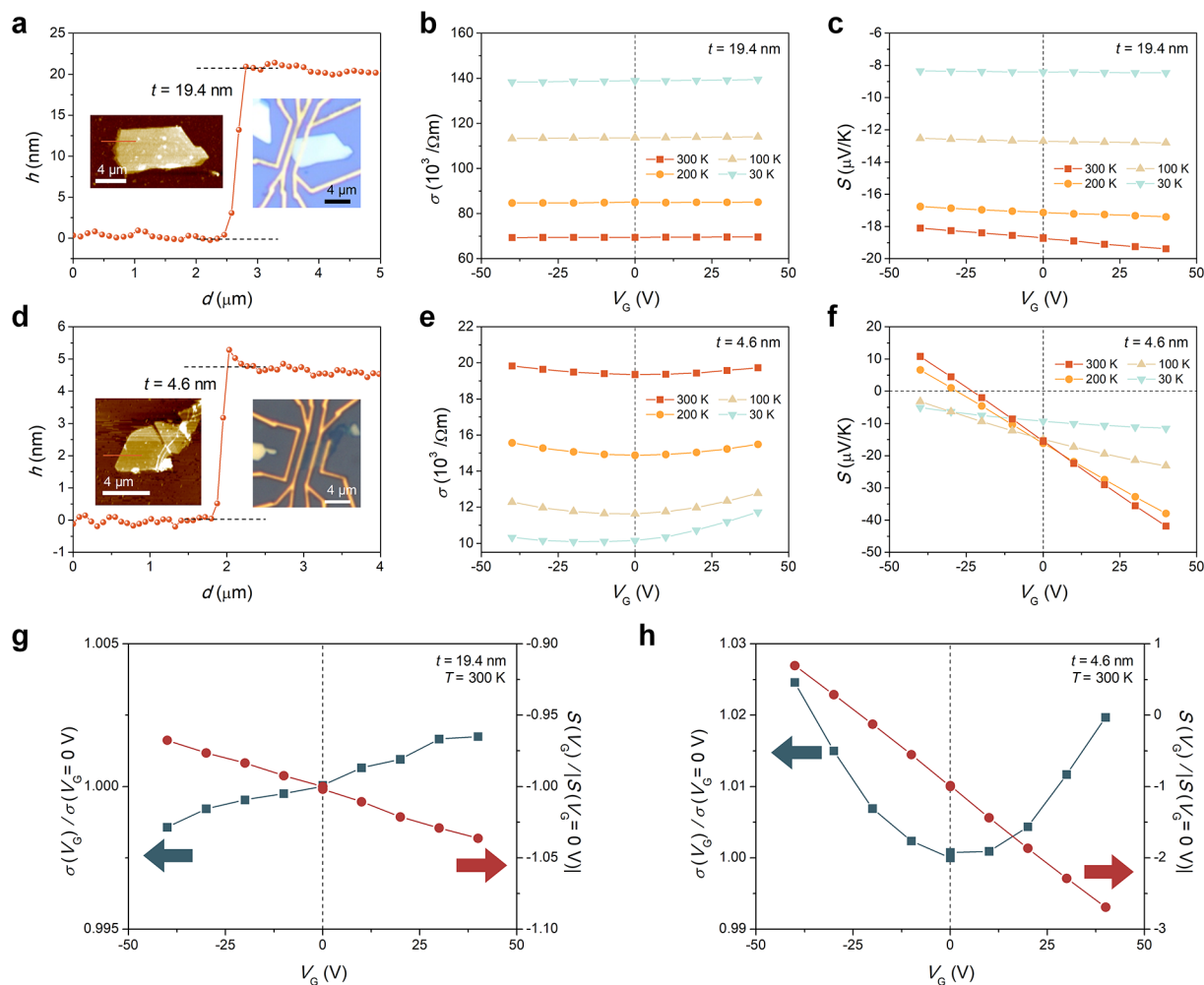


Figure 3. Transport characterization of 19.4 nm-thick and 4.6 nm-thin PtSe₂ nanosheets. (a, d) AFM height profiles of the thick (a) and thin (d) PtSe₂ nanosheets. The left and right insets show the nanosheets before (as a topographic AFM image) and after device fabrication (as an optical image), respectively. (b, e) Gated electrical conductivity of the thick (b) and thin (e) nanosheets at 300 K (red squares), 200 K (orange circles), and 100 K (khaki triangles) and 30 K (light blue downward facing triangles). (c, f) Gated thermopower of the thick (c) and thin (f) nanosheets at the same temperatures. The error bars are smaller than the symbol size. (g, h) Normalized electrical conductivity (dark blue squares) and thermopower (red circles) with respect to the gate voltage of the thick (g) and thin (h) nanosheets at room temperature.

monolayer, resulting in a dramatic thermopower enhancement (Figure S2).

Semimetallic PtSe₂ Nanosheets. To test our theoretical simulations of semimetallic TMDCs and to examine the efficiency of the band engineering approach for transport modulation, we investigated the transport properties of semimetallic PtSe₂ nanosheets with more than three layers. In the following, we refer to PtSe₂ nanosheets with a thickness of 19.4 nm to “thick nanosheets” and to those with a thickness of 4.6 nm to “thin nanosheets”. According to the layer spacing, the layer numbers of the thick and thin nanosheets were estimated to be 38 and 9, respectively. The devices for electrical conductivity and thermopower measurements were fabricated with exfoliated PtSe₂ nanosheets by lithography and metallization after determining the thickness using atomic force microscopy (AFM, Figure 3a,d). The measurement errors were negligible compared to the variation of transport properties according to the temperature and gate voltage (Figures S4–S6). We also found that the transport properties of the PtSe₂ nanosheets were stable and reproducible (Figures S7 and S8).

The electrical conductivity of the thick nanosheets increased with decreasing temperature, and we hardly observed gate-modulated variation (Figure 3b). The sample, thus, exhibited metal-like transport characteristics. These findings indicate that a highly degenerate band structure with sufficient charge density was present and that they are consistent with a previous study on a PtSe₂ nanosheet thicker than 10 nm obtained from the same PtSe₂ crystals.²⁸ Moreover, the carrier-surface scattering in the thick nanosheets was not large enough to suppress the temperature dependence of the carrier mobility, which is the reason why the temperature-dependent electrical conductivity exhibited the metallic behavior.^{17,30} The thermopower of the thick nanosheets showed negative values with very weak gate dependence at the voltage range of –40 to 40 V (Figure 3c), which means that electrons are the major charge carriers. Normalizing the electrical conductivity and thermopower demonstrated a weak gate-modulated character of the thick nanosheets (Figure 3g). The gate-modulated electrical conductivity had a positive slope, which indicates electron-dominant transport; the absolute value of the thermopower increased with increasing electron density. This

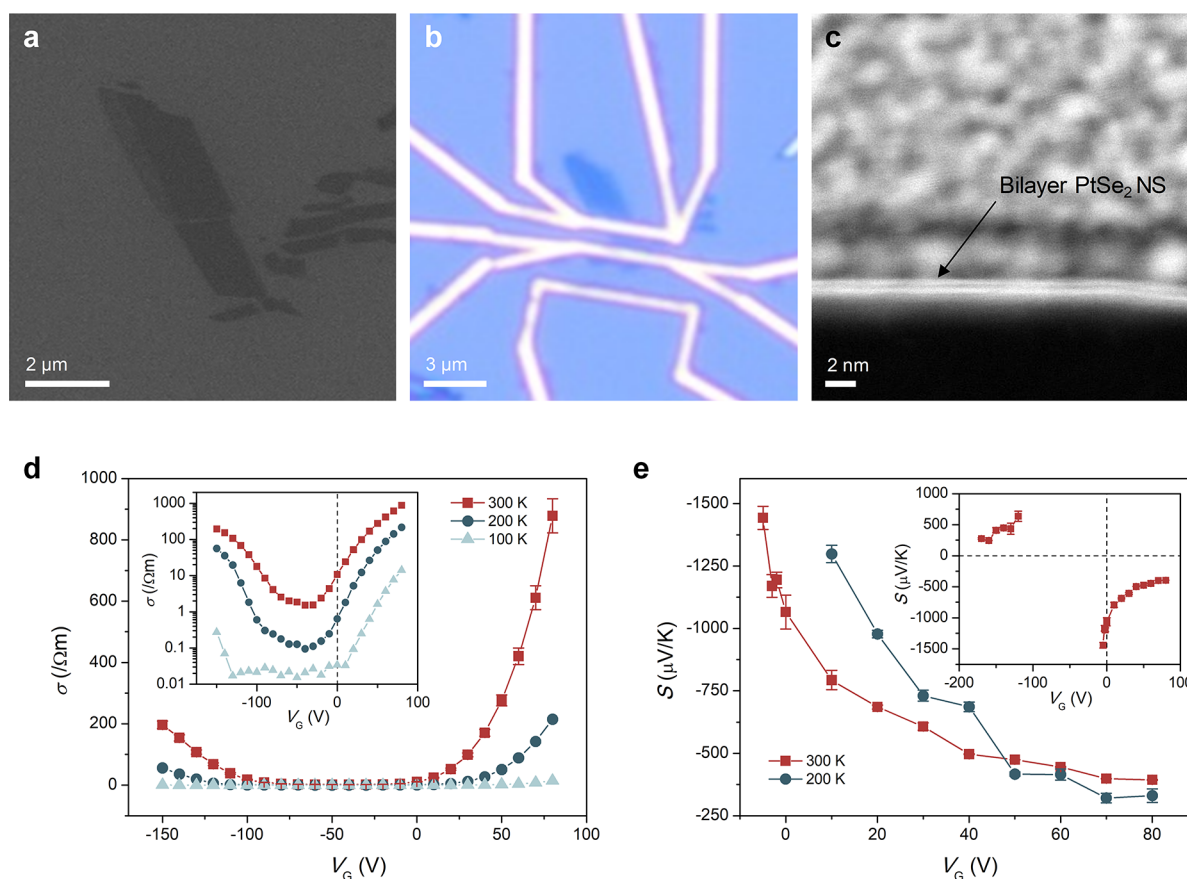


Figure 4. Transport characterization of an ultrathin bilayer PtSe₂ nanosheet. (a) Scanning electron microscopy (SEM) image before device fabrication. (b) Optical image after device fabrication. (c) Cross-sectional STEM image of a vertically sliced specimen of the device after the transport measurements. (d) Gated electrical conductivity at 300 K (red squares), 200 K (dark blue circles), and 100 K (light blue triangles). The inset shows the same graph in log scale. (e) Gated thermopower in a gate voltage range of -5 to 80 V. The inset shows the gated thermopower in the whole tested gate voltage range of -170 to 80 V reflecting the semiconducting band structure.

metal-like behavior was consistently observed in nanosheets thicker than 40 nm (Figure S9) and is in good agreement with the theoretical calculation of the carrier density-dependent transport properties in bulk PtSe₂ (Figure S3).

The gate-modulated electrical conductivity and thermopower of the thin PtSe₂ nanosheets showed ambipolar transport characteristics, as predicted from the semimetallic band structures (Figure 3e, f). The normalized data showed that the electrical conductivity of the thin nanosheet exhibited a u-shape nonmonotonic variation with respect to the gate voltage (Figure 3h). This is a strong evidence for ambipolar transport that is due to an indirect band overlap of semimetals as shown in the theoretical calculation (Figure 2d) and is in good agreement with a previous study using the polymer electrolyte gate effect on 4 and 5 nm nanosheets obtained from the same PtSe₂ crystals.²⁸ The positive and negative slopes of the gate-modulated electrical conductivity indicate electron- and hole-dominant transport, respectively. The thermopower also changed continuously from positive to negative as the gate voltage increased, and the major carriers vary from holes to electrons, as shown in the calculation (Figure 2d). This ambipolar transport behavior can be understood with a two band model in semimetals (Figure S10).^{5,17}

It should be noted that the thick nanosheet with bulk characteristics does not show clear ambipolar transport characteristics even in the semimetallic band structure. This can be attributed to the difference of band overlap energy in

the nanosheets with different thicknesses. As shown in the theoretical predictions, bulk PtSe₂ is also a semimetal (Figure S1) and exhibits ambipolar transport within the energy of the band overlap (Figure S2). However, in terms of a variation in the carrier density, the change in transport properties of bulk PtSe₂ is significantly weaker than that of the trilayer nanosheet (Figure S3). This is because the band overlap energy of bulk PtSe₂ (0.87 eV) is larger than that of the trilayer nanosheets (0.09 eV). The widening band overlap leads to an increase of carrier density.³³ Thus, despite the same variation in carrier density as in the case of the trilayer, only electron dominant transport is observed in the bulk. In the thin nanosheets, a temperature dependence of the electrical conductivity due to thermally excited charge carriers can be observed because the reduced band overlap decreases the carrier density (Figure 3e). The gate-modulated variations of electrical conductivity and thermopower in the thin nanosheet were 10 and 40 times larger than those of the thick nanosheet, respectively (Figure 3g,h). This suggests that the thickness-modulated band engineering based on semimetallic PtSe₂ is sufficient to effectively tune the transport properties in nanosheets.

Semiconducting PtSe₂ Nanosheets. In order to determine the largest thermopower enhancement in PtSe₂ nanosheets and to evaluate potential thermoelectric applications of the thickness-modulated band-engineered semimetallic TMDCs, we investigated the thinnest PtSe₂ nanosheets we were able to produce, a bilayer nanosheet. We first fabricated

the microdevice for transport measurements using this ultrathin nanosheet (Figure 4a,b). The number of layers was determined by cross-sectional STEM of a specimen sliced vertically after the transport measurements because adsorbents on the surfaces of substrate and nanosheet can cause an overestimation of the AFM height profile in atomically thin nanosheets (Figure 4c).^{34,35} The gate-modulated electrical conductivity of the ultrathin nanosheet showed clear semiconducting characteristics with on/off states indicating the formation of a bandgap (Figure 4d).³⁰ We successfully conducted a sufficient gate voltage sweep of -150 to 80 V, and we were able to observe the electron and hole dominant transport on both sides of the bandgap in the temperature range of 100 to 300 K (inset of Figure 4d). This is consistent with the previously observed polymer electrolyte gate effect on a 2.5 nm nanosheet obtained from the same PtSe₂ crystals.²⁸

To confirm the predicted thermopower enhancement, we examined the variation of thermopower with the gate voltage sweep of -5 to 80 V (Figure 4e). As approaching the off state, the absolute value of the thermopower sharply increased to 1.5 mV/K in the measurable range, which is more than 50 times larger than that of the metal-like thick nanosheet. We note that in the off state, the reduced electrical conductivity decreased the signal-to-noise ratio of the thermopower voltage, increasing measurement errors (Figures S4–S6). Furthermore, in the full range gate voltage sweep (-170 to 80 V), we clearly observed the theoretically predicted changes in positive and negative thermopower on both sides of the off state (inset of Figure 4e), which originate from hole and electron bands, respectively (Figure 2c).

Tunable Thermoelectric Performance. Finally, to evaluate the enhancement of thermoelectric performance in thickness-modulated band-engineered PtSe₂ nanosheets, we obtained the power factor from the measured electrical conductivity and thermopower. We fabricated and measured three additional devices with four-probe measurements to eliminate any deviation due to contact resistance and to determine the variation of the power factor originating from the band engineering (Figure S11). Prior to the SMSC transition, the power factor gradually decreased with decreasing nanosheet thickness due to carrier-surface scattering and ambipolar transport, except for the 19.4 nm nanosheet where the electrical conductivity was underestimated owing to contact resistance (Figure 5). However, the variation of the power factor according to the gate voltage increased rapidly with decreasing band overlap energy (inset of Figure 5), and in the bilayer nanosheet, the value sharply increased with increasing gate voltage. Moreover, the rate of change in gated electrical conductivity and thermopower indicated that the power factor of the semiconducting nanosheet can be increased further in a higher gate voltage range (Figure 4d,e). Consequently, we demonstrated the enhancement of the power factor and its tunability using an SMSC transition in semimetallic PtSe₂.

CONCLUSION

Our study demonstrates a dramatic enhancement of thermopower based on thickness-modulated electronic band engineering using two-dimensional nanosheets exfoliated from semimetallic PtSe₂ crystals. The synthetic semiconducting nanosheets obtained by an SMSC transition from semimetallic TMDCs have several advantages for thermoelectric applications such as (1) a large variation of transport properties, (2) a

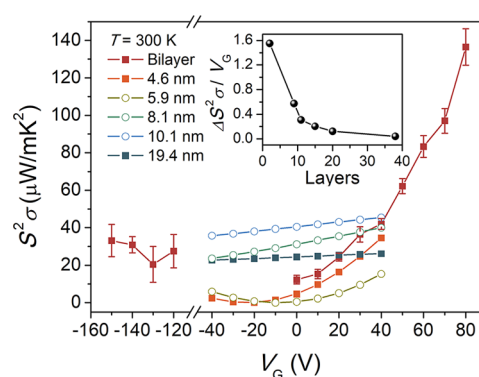


Figure 5. Thermoelectric performance characterization of PtSe₂ nanosheets of different thicknesses. Power factors ($S^2\sigma$) of the bilayer (red squares), 4.6 nm (orange squares), 5.9 nm (yellow circles), 8.1 nm (green circles), 10.1 nm (light blue circles), and 19.4 nm nanosheets (dark blue squares) as a function of the gate voltages at room temperature. Solid and open symbols refer to the use of two- and four-probe measurements to obtain the electrical conductivity, respectively. The error bars were smaller than the symbol size except for the bilayer nanosheet. The inset shows the gate dependence of the power factors as a function of the layer numbers. The unit of $\Delta S^2\sigma/V_G$ is $\mu\text{W}/\text{mK}^2\text{V}$. The numbers of nanosheet layers were estimated based on their thickness according to the lattice constant of *c*.

decrease of the ambipolar transport effect, and (3) a high carrier density dependence of the transport properties. While thick PtSe₂ nanosheets (19.4 nm) showed metal-like characteristics similar to bulk crystals, a semimetallic ambipolar behavior was observed in thin nanosheets (4.6 nm). With an ultrathin nanosheet (bilayer), we were able to observe apparent semiconducting gating characteristics and, as a result, could obtain thermopower values higher than 1 mV/K and an enhanced and tunable power factor. Our observations suggest the development of thermoelectric applications based on thickness-modulated band engineering of other semimetallic TMDCs. We anticipate that even metallic bulk crystals with poor thermoelectric performances are worth studying to develop promising two-dimensional nanostructured thermoelectric materials.

EXPERIMENTAL SECTION

Device Fabrication. PtSe₂ nanosheets were mechanically exfoliated onto a highly doped Si substrate with 300 nm-thick thermally grown SiO₂ using bulk PtSe₂ crystals (HQ Graphene). The layered crystal structure of the exfoliated PtSe₂ nanosheets was characterized using STEM (JEM-ARM 200F, Jeol), dual beam FIB (crossbeam 540, ZEISS), and Raman spectroscopy (LabRam ARAMIS, Horiba Scientific). Thickness measurements using AFM (XE-150, Park Systems) were performed before device fabrication to select nanosheets of the desired thicknesses. Microdevices for transport measurements were fabricated using electron-beam lithography (VEGA3, Tescan and NPGS, JC Nability Lithography Systems) and a lift-off process. To optimize electrical contact between the PtSe₂ and the electrodes, the patterned nanosheet was exposed for 20 s to Ar plasma, followed by a Cr (5 nm)/Au (100 nm) metallization using a custom-made plasma etching and sputtering system. Details of the device fabrication are described in previous reports.^{17,36}

Band Structure and Transport Property Calculations. First-principle DFT calculations were performed using the projector augmented plane-wave method implemented in the Vienna *ab Initio* simulation program code.³⁷ The general gradient approximation with the Perdew–Burke–Ernzerhof functional was used with spin–orbit

coupling.^{38,39} Slab supercells of monolayer, bilayer, and trilayer with a vacuum layer of 15 Å along the *c*-axis were used. van der Waals correction was included using the DFT-D3 method with Becke–Johnson rational damping.^{40,41} A *k*-point mesh of $56 \times 56 \times 1$ was used for the monolayer, bilayer, and trilayer models, and a $28 \times 28 \times 28$ *k*-point mesh was used for the bulk model. The plane-wave basis cutoff energy was set to 700 eV. The structural relaxations were performed until the Hellmann–Feynman forces were $<10^{-5}$ eVÅ⁻¹. The electrical conductivity and the thermoelectric power were estimated using the Shankland–Koelling–Wood interpolation as implemented in the BoltzTraP2 code.^{42,43}

Transport Property Measurements. The microdevice for transport property measurements consisted of a microheater and two thermometers. The electrical conductivity was obtained by *I*–*V* and *V*–*I* measurement systems (236 and 2182, Keithley) for low-resistance metal-like and semimetallic nanosheets and for high-resistance semiconducting nanosheets, respectively. For the thermopower measurement, the voltage difference between two thermometers was measured by a nanovoltmeter (2182, Keithley). The temperature difference was calibrated using the temperature coefficient of the resistance of each thermometer, which was measured by a lock-in amplifier (SR850, Stanford Research Systems) during Joule heating of the microheater. All measurements including the temperature-dependent properties were conducted using a closed cycle cryostat (X-IAL, Advanced Research Systems) in a high vacuum of $<5 \times 10^{-6}$ Torr without convective thermal fluctuation. A detailed description of the transport measurements based on single nanosheets is available in the Supporting Information (Figures S4–S6) and previous studies.^{17,32}

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsnano.9b06523.

Calculated electronic band structures, DOS, and transport properties for monolayer, bilayer, trilayer nanosheets, and bulk crystal, measurement techniques and errors with representative raw data, four-probe measurements and contact resistance, stability and reproducibility of PtSe₂ nanosheets, transport properties of a metal-like 40 nm nanosheet, and simple two band model in transport properties of semimetals (PDF)

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Notes

The authors declare no competing financial interest.

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